MATHEMATICS ACHIEVEMENT IN THE PRIMARY SCHOOL YEARS:
IEA’S THIRD INTERNATIONAL MATHEMATICS AND SCIENCE STUDY (TIMSS)

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- Developing the TIMSS Mathematics Test
- TIMSS Test Design
- Sample Implementation and Participation Rates
- Indicating Compliance with Sampling Guidelines in the Report
- Data Collection